# Variation using a maths GCSE question 

Year 11 (Higher)

HIAS Maths Team (secondary)
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Final version
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## Overview

## This document contains...

A set of connected questions that link to a past GCSE question

## Points to consider when using this resource

Each variation of the exam question should be considered as part of a learning journey. Teachers may wish to consider models and images to support students to access the problems.

## Year 11 H: variation: Edexcel 2018 P3 Q13

## Similar shapes

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## Prior knowledge to review

- Multiplication strategies
- Surds
- Length , area and volume scale factors
- Surface area
- Volume


A
B

Here are two similar solid shapes
height of shape $\mathbf{A}$ : height of shape $\mathbf{B}=2: 1$
The surface area of shape B is $20 \mathrm{~cm}^{2}$
Work out the surface area of shape $\mathbf{A}$


A
B

Here are two similar solid shapes
height of shape $\mathbf{A}$ : height of shape $\mathbf{B}=2: 1$
The surface area of shape $\mathbf{B}$ is $20 \mathrm{~cm}^{2}$
Work out the surface area of shape $\mathbf{A}$

Linear scale factor $=2: 1$
Area scale factor $=2^{2}: 1^{2}=4: 1$
Surface area $A: B=80: 20$
The surface area of shape $\mathbf{A}$ is $80 \mathrm{~cm}^{2}$

Here are two similar solid shapes
surface area of shape $\mathbf{A}$ : surface area of shape $\mathbf{B}=1: 16$
The height of shape $\mathbf{B}$ is 20 cm
Work out the height of shape A


A


B

## Solution <br> B <br> 

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Here are two similar solid shapes
surface area of shape $\mathbf{A}$ : surface area of shape $\mathbf{B}=1: 16$
The height of shape $\mathbf{B}$ is 20 cm
Work out the height of shape A

Area scale factor $=1: 16=1^{2}: 4^{2}$
Linear scale factor $=1: 4$
Height $A: B=5: 20$
The height of shape $\mathbf{A}$ is 5 cm


A


B

Here are two similar solid shapes
width of shape $\mathbf{A}$ : width of shape $\mathbf{B}=3: 4$
The volume of shape $\mathbf{B}$ is $32 \mathrm{~cm}^{3}$
Work out the volume of shape $\mathbf{A}$

## Solution

Here are two similar solid shapes
width of shape $\mathbf{A}$ : width of shape $\mathbf{B}=3: 4$
The volume of shape $\mathbf{B}$ is $32 \mathrm{~cm}^{3}$
Work out the volume of shape $\mathbf{A}$

Linear scale factor $=3: 4$
Volume scale factor $=3^{3}: 4^{3}=27: 64$
Volume A : Volume B = 13.5 : 32
The volume of shape $\mathbf{A}$ is $13.5 \mathrm{~cm}^{3}$

Here are two similar solid shapes
surface area of shape $\mathbf{A}$ : surface of shape $\mathbf{B}=16: 9$
The volume of shape $\mathbf{B}$ is $5.4 \mathrm{~cm}^{3}$
Work out the volume of shape $\mathbf{A}$


A


B

Solution
Here are two similar solid shapes


A
surface area of shape $\mathbf{A}$ : surface of shape $\mathbf{B}=16: 9$
The volume of shape $\mathbf{B}$ is $5.4 \mathrm{~cm}^{3}$
Work out the volume of shape $\mathbf{A}$

B
Area scale factor $A: B=16: 9$
Linear scale factor $A: B=\sqrt{16}: \sqrt{9}=4: 3$
Volume scale factor $A: B=4^{3}: 3^{3}=64: 27$
$27 \div 5.4=5$

Here are two similar solid shapes


B
surface area of shape $\mathbf{A}$ : surface of shape $\mathbf{B}=7: 1$
The volume of shape $\mathbf{B}$ is $15 \mathrm{~cm}^{3}$
Work out the volume of shape $\mathbf{A}$
Give your answer to 3 significant figures

Solution


A

Here are two similar solid shapes
surface area of shape $\mathbf{A}$ : surface of shape $\mathbf{B}=7: 1$
The volume of shape $\mathbf{B}$ is $15 \mathrm{~cm}^{3}$
Work out the volume of shape $\mathbf{A}$
Give your answer to 3 significant figures

B
Area scale factor $\mathrm{A}: \mathrm{B}=7: 1$
Linear scale factor $A: B=\sqrt{7}: \sqrt{1}$
Volume scale factor $A: B=(\sqrt{7})^{3}:(\sqrt{1})^{3}=7 \sqrt{7}: 1$
(Vol) A : (Vol) B $=7 \sqrt{7}: 1=(15 \times 7 \sqrt{7}):(15 \times 1)$

Edexcel : H: 2018: P3: Q13

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(3 marks)

Here are two similar solid shapes.

surface area of shape $\mathbf{A}$ : surface area of shape $\mathbf{B}=3: 4$
The volume of shape B is $10 \mathrm{~cm}^{3}$
Work out the volume of shape $\mathbf{A}$.
Give your answer correct to 3 significant figures.

Edexcel : H: 2018: P3: Q13

## Solution

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Here are two similar solid shapes.
A
B

Area scale factor $A: B=3: 4$
Linear scale factor $A: B=\sqrt{3}: \sqrt{4}$
Volume scale factor $A: B=(\sqrt{3})^{3}:(\sqrt{4})^{3}=3 \sqrt{3}: 8$
Since $8 \times 1.25=10\left(\right.$ volume of $B$ is $\left.10 \mathrm{~cm}^{3}\right)$
Then $3 \sqrt{3} \times 1.25=6.49519 \ldots=6.50 \mathrm{~cm}^{3}$ to 3 sig figs
surface area of shape $\mathbf{A}$ : surface area of shape $\mathbf{B}=3: 4$
The volume of shape $\mathbf{B}$ is $10 \mathrm{~cm}^{3}$
Work out the volume of shape $\mathbf{A}$.
Give your answer correct to 3 significant figures.

## HIAS Maths Team (secondary)

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